

# The Mystery of Dark Matter: the Galactic Rotation Curve for the Milky Way

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## **Abstract**

Dark matter is one of the most mysterious presences known to science. Its existence can only be deduced from other data. One of those forms of data is the galactic rotation curve. In order to ascertain the presence of dark matter in our own galaxy, velocities and distances to the galactic center for selected points will be made. Once observations and calculations are complete, the results indicate the existence of dark matter in the Milky Way Galaxy.

## **Introduction**

What is dark matter? Essentially, it can be defined as matter that exerts a gravitational effect upon other matter but is not currently detectable. Dark matter is theorized to have at least two forms: hot and cold. Hot dark matter has an extremely low mass, but moves at extremely high speeds. Hot dark matter could potentially consist of particles like neutrinos. Conversely, cold dark matter has a high mass, but moves at very low speeds. It might be made up of particles like WIMPs, or Weakly Interacting Massive Particles. In addition, dark matter can possibly be either baryonic matter or non-baryonic matter. Baryonic candidates, those objects that are made up of atoms, include brown dwarfs, dim nebulae and stars, or black holes. Non-baryonic candidates, those previously mentioned as hot or cold dark matter, might even include an unknown form of matter.

Regardless, dark matter is a poorly known substance, still in theoretical status, that could be several objects.

The presence of dark matter can be inferred from other data, such as rotation speeds of stars that are higher than predicted, gravitational lensing, and the formation of universal structures (with the amount of gravity provided by luminous matter, the universal structures would not form). This inference leads to the purpose of the project, which is to calculate the rotation curve of the Milky Way Galaxy and thus ascertain the presence of dark matter in the galaxy.

### Method

A certain procedure was used in collecting data and calculating results. First, points to observe were chosen. All chosen points had a galactic latitude equivalent to  $0^\circ$ ; galactic longitudes started at  $0^\circ$  and varied by  $10^\circ$  up to  $350^\circ$ . Second, these points were converted to the equatorial system to meet the parameters of the 4.6 meter radio telescope used to obtain data. The telescope is nicknamed Smiley and is located at the Pisgah Astronomical Research Institute near Rosman, North Carolina. The conversion of the points was accomplished via the following equations:

$$\sin(\zeta) = \cos(b^{\text{II}})\sin(l^{\text{II}}-33)\sin(62.6) + \sin(b^{\text{II}})\cos(62.6) \text{ and}$$

$$\cos(\zeta)\sin(\alpha-282.25) = \cos(b^{\text{II}})\sin(l^{\text{II}}-33)\cos(62.6) - \sin(b^{\text{II}})\sin(62.6)$$

where  $\zeta$  represents declination,  $\alpha$  represents right ascension,  $b^{\text{II}}$  represents galactic latitude, and  $l^{\text{II}}$  represents galactic longitude. The original points in the galactic system (measured in degrees) and the converted points in the equatorial system (right

ascension in hours, minutes, and seconds, and declination in degrees, arcminutes, and arcseconds) are in Table 1 as follows:

Table 1- Points and Converted Points

| Galactic Latitude | Galactic longitude | Right ascension | Declination. |
|-------------------|--------------------|-----------------|--------------|
| 0                 | 0                  | 17 42 26.6      | -285500.1    |
| 0                 | 10                 | 18 04 47.2      | -201751.3    |
| 0                 | 20                 | 18 24 44.5      | -113113.1    |
| 0                 | 30                 | 18 43 28.4      | -23947.5     |
| 0                 | 40                 | 19 13 59.6      | 6 12 41      |
| 0                 | 50                 | 19 21 02.1      | 15 02 40.9   |
| 0                 | 60                 | 20 33 31.3      | 23 45 57.6   |
| 0                 | 70                 | 20 05 30.2      | 32 17 47.4   |
| 0                 | 80                 | 22 43 29.5      | 40 29 21.5   |
| 0                 | 90                 | 21 10 17.5      | 48 07 24.2   |
| 0                 | 100                | 21 55           | 54 48 33.4   |
| 0                 | 110                | 22 59           | 59 53 22.7   |
| 0                 | 120                | 00 24           | 62 26 56     |
| 0                 | 130                | 01 42           | 61 47 13.9   |
| 0                 | 140                | 03 07           | 58 06 19.7   |
| 0                 | 150                | 03 59           | 52 17 01.2   |
| 0                 | 160                | 04 39           | 45 09 24.9   |
| 0                 | 170                | 05 26           | 37 15 50.4   |
| 0                 | 180                | 05 49           | 28 55 00.4   |
| 0                 | 190                | 06 08           | 20 17 51.5   |
| 0                 | 200                | 06 27           | 11 31 13.1   |
| 0                 | 210                | 06 44           | 02 39 47.5   |
| 0                 | 220                | 07 01           | -61241       |
| 0                 | 230                | 07 24           | -150240.9    |
| 0                 | 240                | 07 43           | -234557.6    |
| 0                 | 250                | 08 04           | -321747.4    |
| 0                 | 260                | 08 37           | -402921.5    |
| 0                 | 270                | 09 12           | -480724.2    |
| 0                 | 280                | 10 01           | -544833.4    |
| 0                 | 290                | 11 06           | -595322.7    |
| 0                 | 300                | 12 08           | -622656      |
| 0                 | 310                | 13 51           | -614713.9    |
| 0                 | 320                | 15 03           | -580619.7    |
| 0                 | 330                | 15 59           | -521701.2    |
| 0                 | 340                | 16 02           | -450924.9    |
| 0                 | 350                | 17 11           | -371550.4    |

Third, 21 chosen points were observed. Because of equipment and location limitations, it was not possible to observe certain points. The points actually observed are in Table 2 as follows:

Table 2- Observed Points (in degrees)

| gal. lat. | gal. long. |
|-----------|------------|
| 0         | 10         |
| 0         | 20         |
| 0         | 30         |
| 0         | 40         |
| 0         | 50         |
| 0         | 60         |
| 0         | 70         |
| 0         | 80         |
| 0         | 90         |
| 0         | 100        |
| 0         | 110        |
| 0         | 120        |
| 0         | 130        |
| 0         | 140        |
| 0         | 150        |
| 0         | 160        |
| 0         | 170        |
| 0         | 210        |
| 0         | 220        |
| 0         | 230        |
| 0         | 240        |

The above points were, in equatorial form, entered into the controls of the 4.6 meter radio telescope. Scans of neutral hydrogen in the 2.7 degree range of the telescope for each point were conducted. The value where the neutral hydrogen intensity peaked (in Megahertz) was used in the following formula to obtain a raw radial velocity:

$f/1420.406 \text{ MHz} (c)$  where **f** is frequency in Megahertz and **c** is the speed of light (300,000 km/s). These velocities are in Table 3 below.

Table 3- Raw Radial Velocities

| Galactic Longitude | Radial Velocity (in km/s) |
|--------------------|---------------------------|
|--------------------|---------------------------|

|           |         |
|-----------|---------|
| (degrees) |         |
| 10        | 4.224   |
| 20        | 16.897  |
| 30        | 21.103  |
| 40        | 23.233  |
| 50        | 25.345  |
| 60        | 29.569  |
| 70        | 27.457  |
| 80        | 35.905  |
| 90        | 31.681  |
| 100       | 32.737  |
| 110       | 33.793  |
| 120       | 31.681  |
| 130       | 25.345  |
| 140       | 16.897  |
| 150       | 19.009  |
| 160       | 21.121  |
| 170       | 8.448   |
| 210       | -33.793 |
| 220       | -38.017 |
| 230       | -52.802 |
| 240       | -46.466 |

The above raw velocities were corrected for the motion of the Local Standard of Rest (LSR) and for heliocentric velocity. To correct for the LSR motion, a website program<sup>1</sup> was used; to correct for the heliocentric velocity, an IRAF program put out by the NOAO was used. Velocities after 1) being corrected for LSR motion and 2) after being corrected for both the LSR motion and heliocentric velocity are displayed in (respectively) Tables 4 and 5 below.

Table 4- Velocities Corrected for LSR motion

| Galactic Longitude (degrees) | LSR-corrected Velocities (km/s) |
|------------------------------|---------------------------------|
| 10                           | -8.746                          |
| 20                           | -.703                           |
| 30                           | -.657                           |
| 40                           | -3.177                          |
| 50                           | -2.595                          |
| 60                           | -3.471                          |

<sup>1</sup> [fuse.pha.jhu.edu/support/tools/vlsr.html](http://fuse.pha.jhu.edu/support/tools/vlsr.html)

|     |         |
|-----|---------|
| 70  | -3.293  |
| 80  | 3.765   |
| 90  | 1.811   |
| 100 | 4.637   |
| 110 | 8.393   |
| 120 | 10.011  |
| 130 | 7.375   |
| 140 | 4.327   |
| 150 | 10.569  |
| 160 | 17.551  |
| 170 | 11.988  |
| 210 | -11.783 |
| 220 | -12.727 |
| 230 | -24.522 |
| 240 | -16.586 |

Table 5- Final Velocities Corrected for LSR Motion and Heliocentric Velocity

| Galactic<br>Longitude<br>(degrees) | Velocity(km/s) |
|------------------------------------|----------------|
| 10                                 | 3.9            |
| 20                                 | 19.2           |
| 30                                 | 25.3           |
| 40                                 | 31.9           |
| 50                                 | 34.6           |
| 60                                 | 46.0           |
| 70                                 | 40.1           |
| 80                                 | 57.3           |
| 90                                 | 46.2           |
| 100                                | 47.4           |
| 110                                | 48.0           |
| 120                                | 45.2           |
| 130                                | 37.9           |
| 140                                | 27.7           |
| 150                                | 28.8           |
| 160                                | 29.2           |
| 170                                | 12.9           |
| 210                                | 39.2           |
| 220                                | 45.5           |
| 230                                | 62.8           |
| 240                                | 58.0           |

The final velocities were plotted in a velocity curve (absolute value was taken of all to eliminate negatives). **All velocities have an uncertainty of + or – 1.1.** Next, the

observed points' distance from the galactic center ( $R_{min}$ ) was calculated using the following equation:

$R_{min}=R_o(\sin l)$  where  $R_{min}$  is the distance from the galactic center,  $R_o$  is equivalent to 8 kiloparsecs, and  $l$  is the galactic longitude. Table 6 charts the obtained distances in kiloparsecs as follows:

Table 6- Distance from the Galactic Center

| Galactic Longitude (degrees) | Distance (kpc) |
|------------------------------|----------------|
| 10                           | 1.389          |
| 20                           | 2.736          |
| 30                           | 4.000          |
| 40                           | 5.142          |
| 50                           | 6.128          |
| 60                           | 6.928          |
| 70                           | 7.518          |
| 80                           | 7.878          |
| 90                           | 8.000          |
| 100                          | 7.878          |
| 110                          | 7.518          |
| 120                          | 6.928          |
| 130                          | 6.128          |
| 140                          | 5.142          |
| 150                          | 4.000          |
| 160                          | 2.736          |
| 170                          | 1.389          |
| 210                          | 4.000          |
| 220                          | 5.142          |
| 230                          | 6.128          |
| 240                          | 6.928          |

Absolute value was taken of all distances to eliminate negative values. A rotation curve for the Milky Way Galaxy, with velocity as a function of distance from the galactic center, was then plotted. To demonstrate the presence of dark matter, a Keplerian rotation curve was plotted on top of the Milky Way rotation curve. The equation for calculating the Keplerian rotation curve is as follows:

$\sqrt{(GM)/R}$  where  $G$  is the gravitational constant,  $M$  is  $10^{10}$  solar masses, and  $R$  is the distance from the galactic center in meters. (Answers should be converted to km/s

because meter was used to cancel units.) Table 7 below contains the values obtained for the Keplerian Rotation Curve.

Table 7- Keplerian Rotation Curve Values

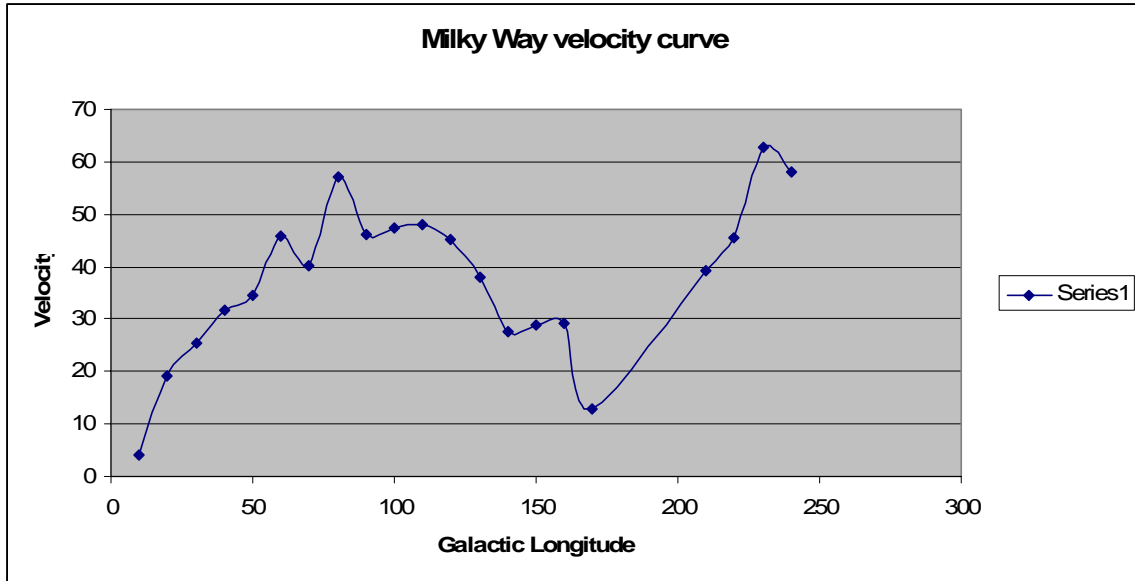
| Distance<br>from the<br>Galactic<br>Center<br>(kpc) | Velocity(km/s) |
|---|----------------|
| 8   | 73.39          |
| 9   | 69.19          |
| 12  | 59.92          |
| 15  | 53.60          |
| 18  | 48.93          |

The two different rotation curves for the Milky Way Galaxy were compared to ascertain the presence of dark matter.

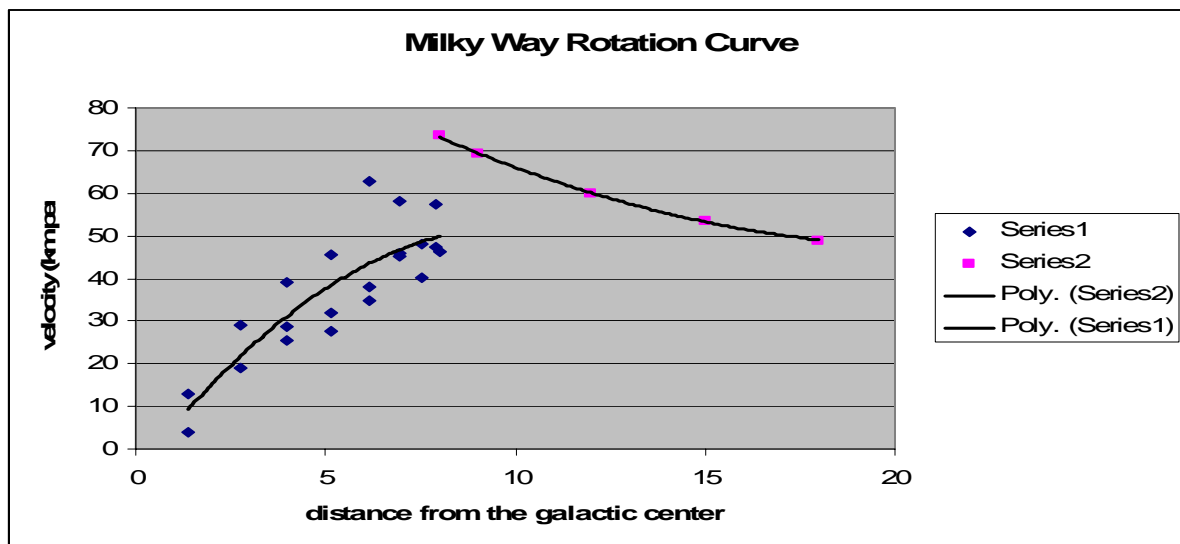
### Results

Because of the nature of the Smiley telescope scans, it is not possible to include them. However, the link to them is as follows:

<http://smiley.pari.edu:8080/smiley/analyze/mainpanel.html> (scroll on the drop-down menu to tip2006; the data are labeled as [coordinates] DK scan). The velocity curve obtained is below, with velocity in km/s and galactic longitude in degrees.



This curve indicates that different points in the galaxy have varying velocities, spanning from about 4 to 64 Km/sec. This fact stems from the various natures of the galactic objects. The rotation curves obtained are below. Blue is the observed rotation curve, and pink is the Keplerian rotation curve. Velocity is in km/s; distance from the galactic center is in kpc.



The observed curve had an overall upward trend, leveling off toward the end of observed data. The Keplerian curve had a gradual downward trend, also leveling off

toward the end of calculated data. If the trends continue, the observed rotation curve should cross the Keplerian curve somewhere between 10 and 15 kiloparsecs. This occurrence would indicate the presence of some unknown type of matter-dark matter.

### **Discussion**

As with most projects, some assumptions, approximations, and limitations were present. First, more data points of velocity would be useful; because of latitudinal and telescope limitations, some points could not be observed. These extra points of data would confirm the hypothesis that the trend lines of the two rotation curves would cross, with the observed rotation curve becoming higher than the Keplerian curve. Second, most data points were rounded to two or three significant places. Third, the distance from the galactic center and the measured velocity were assumed to be perpendicular and thus at the tangent point of an object's orbit. Fourth, all formulae used were assumed to be correct; the telescope was assumed to be functioning correctly.

In addition, the results obtained are comparable to other available data. However, this project could be improved through more collection of data from a different location, as well as a longer time to collect data. The short time inhibited the project. Nevertheless, meaningful data were still able to be obtained.

### **Conclusion**

In order to determine the presence of dark matter in the Milky Way Galaxy, velocities and distances from the galactic center for selected points were measured and calculated. Next, an observational rotation curve and a calculated Keplerian rotation curve were made. The comparison of the two corroborates the presence of extra or dark matter in the universe. This dark matter could be any number of objects in our galaxy, or

something completely unknown; nevertheless, it encompasses one of the mysteries of the universe.

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